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Application of Shortest Path

Aye Aye Myint
Myanmar Institute of Information
Technology
aye_aye_myint@mmit.edu.mm

Myat Moe Khaing
Myanmar Institute of Information
Technology
myat_moe_khaing@mmit.edu.mm

Wai Zin Phyo
Myanmar Institute of Information
Technology
wai_zin_phyo@mmit.edu.mm

Abstract. In this paper, a shortest path algorithm was studied. Firstly, the basic definitions of graph theory such as graph, directed graph (or digraph), weighted graph, path and shortest path will be introduced. Then the shortest path algorithm of Dijkstra into the MATLAB computer program was coded and applied it to the real road network of some towns in the Sagaing division so that there are two places in the region. This program tests the road-network which includes 16 junctions and 28 road-segments. It is hoped that the program would be applied on road-networks of a city or of larger sizes.

Keywords: graph, digraph, weighted graph, path, shortest path.

I. INTRODUCTION

In the city with road-networks, the shortest route between every two locations is useful and important from economic and other points of view. Using a shortest path from one location to the other, a person or an organization may save his or its time, cost and other resources.

A weighted graph is a graph in which edge values are allocated and a path length in a weighted graph is the sum of edge weights in the route. A path with a minimum distance between two specified vertices is called a shortest path in the weighted graph. The shortest path problems are the most significant issues of actual world optimization because they can be formulated and solved as shortest path problems.

II. GRAPH THEORY DEFINITIONS

A. Graph

A **graph** $G = (V, E)$ is a non-empty set of vertices (or nodes) and a set of edges (or arcs). An unordered pair of vertices is connected with each edge. If edge e is connected to vertices v and w , an edge e is connected (v, w) or (w, v) . A graph like this is shown in Figure 1.

B. Digraph

A **digraph** $D = (V, E)$ comprises of a non-empty set V of vertices (or nodes) and a set E of separated edges (or arcs). An ordered pair of vertices is connected with each edge. If it connects to the ordered pair (v, w) of vertices, the edge e is denoted (v, w) . In the Figure 2, $e_1=(v, u)$, $e_2=(w, u)$, $e_3=(z, w)$, $e_4=(v, v)$, $e_5=(w, v)$, $e_6=(v, w)$. D is a simple digraph if all of D 's arcs are separate and there are no loops.



Fig. 1. Graph with $V = \{u, v, w, x\}$ and $E = \{e_1, e_2, e_3, e_4, e_5, e_6, e_7\}$



Fig. 2. Digraph with $V = \{u, v, w, x\}$ and $E = \{e_1, e_2, e_3, e_4, e_5, e_6, e_7\}$

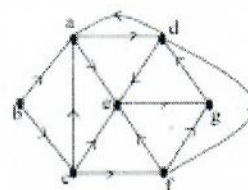


Fig. 3. A Simple digraph

C. Weighted Graph

A real number, called its **weight**, can be connected with each arc of a digraph D . Then D is called a **weighted digraph** along with these weights on its arcs. In most applications weights are positive values.

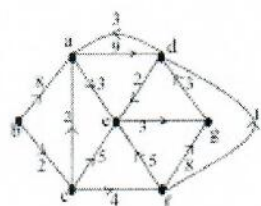


Fig. 4. A weighted graph with weights

D. Path and Shortest Path

If a person goes on a journey that starts in a certain town, runs through several towns and ends in a certain town, a person must know a path and a shortest path.

An alternating sequence of $n-1$ vertices and n edges starting with vertex v_0 and ending with vertex v_n is a **path** between two designated vertices v_0 and v_n with length n .

denoted by $(V_0, e_1, V_1, e_2, V_2, \dots, V_{n-1}, e_n, V_n)$ where e_i connects with V_{i-1} and V_i for $i=1, 2, \dots, n$.

A path with a minimum distance between two specified vertices is called a **shortest path** in the weighted graph.

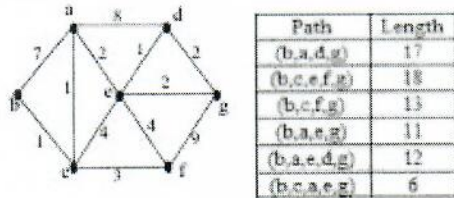


Fig. 5. Weighted graph with path

III. DIJKSTRA'S ALGORITHM

Dijkstra's algorithm finds the length of a shortest path and shortest distance from any vertex to other vertex in a connected and weighted graph.

E. Procedure

Suppose G is a connected weighted graph with vertex set $V = \{v_1, \dots, v_n\}$ in which all weights are positive and let $L(v_i)$ be the label of the vertex v_i and the weight of edge connects with v_i and v_j be greater than zero.

Dijkstra's algorithm finds the shortest distance and shortest path by adding vertices v_1, \dots, v_n into the this path as follow:

Starts with the weighted $n \times n$ matrix of a simple weighted digraph or weighted graph, $M=(a_{ij})$,

where a_{ij} = the weight of the edge from vertex v_i to vertex v_j ,

$a_{ii} = 0$,

$a_{ij} = \infty$, if there is no edge from vertex v_i to vertex v_j ,

and n is the number of vertices.

Set $L(v_1) = 0$ and $L(v_i) = \infty$ for all vertices $v_i \neq v_1$.

$k = 2, \dots, n$.

Then choose vertex v_k adjacent to v_1 with minimum $L(v_k)$ by using the equation

$$L(v_k) = \min \{L(v_2), L(v_1) + \text{weight}(v_1, v_2)\}.$$

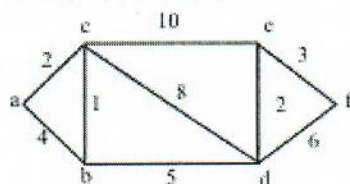
That is, in step 1, vertex v_k is inserted in the path from vertex v_1 to vertex v_n .

In step 2, vertex v_2 is inserted in this path.

Continuing in this way, at termination, $L(v_n)$ is the length of a shortest path from vertex v_1 to vertex v_n .

F. Example

Consider G is a weighted graph:



Let $L(f)$ is the shortest distance from vertex a to vertex f .

TABLE I. PATH LENGTH TABLE

Path	L(b)	L(c)	L(d)	L(e)	L(f)
(a)	4	2	∞	∞	∞
(a, c)	3	-	10	12	∞
(a, c, b)	-	-	8	12	∞
(a, c, b, d)	-	-	-	10	14
(a, c, b, d, e)	-	-	-	-	13
(a, c, b, d, e, f)	-	-	-	-	13

From the above table, the shortest distance is 13 and shortest path is (a, c, b, d, e, f).

IV. CODING DIJKSTRA'S ALGORITHM

There are several computer programs in the graph that find a shortest distance and a shortest path between two vertices.

The shortest path algorithm of Dijkstra into the MATLAB computer program was coded as follow:

function [d P] = dijkstralgorithm(G,start,destin)

if start==destin

d=0;

P=[start];

else

G = drawgraph(G,inf,1);

if destin==1

destin=start;

end

G=RowColchange(G,1,start);

lengthA=size(G,1);

Width=zeros(lengthA);

for i=2 : lengthA

Width(1,i)=i;

Width(2,i)=G(1,i);

end

for i=1 : lengthA

Dis(i,1)=G(1,i);

Dis(i,2)=i;

end

D2=Dis(2:length(Dis),:);

P=2;

while P<=(size(Width,1)-1)

P=P+1;

D2=sortrows(D2,1);

k=D2(1,2);

Width(P,1)=k;

D2(1,:)=[];

for i=1 : size(D2,1)

if Dis(D2(i,2),1)>(Dis(k,1)+G(k,D2(i,2)))

Dis(D2(i,2),1) = Dis(k,1)+G(k,D2(i,2));

D2(i,1) = Dis(D2(i,2),1);

end

end

for i=2 : length(G)

Width(P,i)=Dis(i,1);

end

end

if destin==start

P=[1];

else

P=[destin];

end

e=Width(size(Width,1),destin);

```

P = listalgorithm(P,Width,start,destin);
end
end
function G = RowColchange(G,a,b)
%Exchange element at column;
buffer=G(:,a);
G(:,a)=G(:,b);
G(:,b)=buffer;
%Exchange element at row;
buffer=G(a,:);
G(a,:)=G(b,:);
G(b,:)=buffer;
end
function L = listalgorithm(L,W,s,d)
index=size(W,1);
while index>0
    if W(2,d)==W(size(W,1),d)
        L=[L s];
        index=0;
    else
        index2=size(W,1);
        while index2>0
            if W(index2,d)<W(index2-1,d)
                L=[L W(index2,1)];
                L=listalgorithm(L,W,s,W(index2,1));
                index2=0;
            else
                index2=index2-1;
            end
        end
        index=0;
    end
end
end
function G = drawgraph(G,b,s)
if s==1
    for i=1 : size(G,1)
        for j=1 : size(G,1)
            if G(i,j)==0
                G(i,j)=b;
            end
        end
    end
end
if s==2
    for i=1 : size(G,1)
        for j=1 : size(G,1)
            if G(i,j)==b
                G(i,j)=0;
            end
        end
    end
end
end
end

```

G. Example

Suppose G is a weighted graph in below.

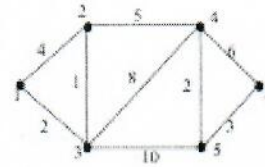


Fig. 6. Weighted graph with weights

Input the data:

```

G=[0 4 2 0 0 0; 4 0 1 5 0 0; 2 1 0 8 10 0; 0 5 8 0 2 6;
   0 0 10 2 0 3; 0 0 0 6 3 0];
[d P] = dijkstra(G,1,6)
The result is
d = 13
P = 1 3 2 4 5 6

```

That is, the shortest distance and shortest path from vertex 1 to vertex 6 are 13 and (1, 3, 2, 4, 5, 6) respectively.

V. SOME RESULTS AND FINDINGS

In this paper, the program with partial road-networks of some towns in Sagaing division was tested. Such a partial road-network with 16 towns and 28 road-segments is shown in Fig.7. Here the road-lengths are in kilometers. The list representation for this partial road-network is shown in Table II. (See in Page. 5)

- Let Ayadaw = vertex 1
- Budalin = vertex 2
- Tabayin = vertex 3
- Ye-U = vertex 4
- Shwebo = vertex 5
- Mynmu = vertex 6
- Chaung-U= vertex 7
- Monywa = vertex 8
- Kani = vertex 9
- Khin-U = vertex 10
- Wetlet = vertex 11
- Sagaing = vertex 12
- Myaung = vertex 13
- Salingyi = vertex 14
- Pale = vertex 15
- Yinmarpin = vertex 16.

```

Input data:
s = [1 1 1 1 1 1 1 2 2 2 3 4 4 5 5 11 11 12 6 6 7 7 8 8
     16 16 16 14];
t = [2 3 4 5 6 7 8 3 8 9 4 5 10 10 11 6 12 6 7 13 8 13
     14 16 9 14 15 15];
weights = [51 70 84 60 46 65 43 38 32 33 14 37 21 35
           37 88 74 60 37 27 22 33 19 47 32 36 19 35];

```

By using the technical tool in Matlab, the result plot is the partial road-network with 16 towns and 28 road-segments shown in Figure 7.

The result plot:

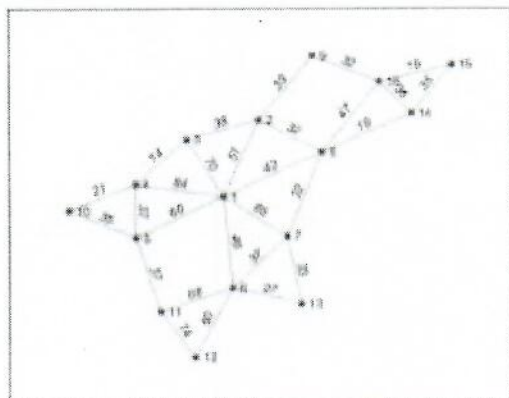


Fig. 7. A partial road-network of Sagaing division

The shortest distance and shortest path between two specified towns will be calculated by using Matlab computer program.

Input the data:

```
G = [0 51 70 84 60 46 65 43 0 0 0 0 0 0 0;
      51 0 38 0 0 0 0 32 33 0 0 0 0 0 0;
      70 38 0 14 0 0 0 0 0 0 0 0 0 0 0;
      84 0 14 0 37 0 0 0 0 21 0 0 0 0 0;
      60 0 0 37 0 0 0 0 0 35 37 0 0 0 0;
      46 0 0 0 0 37 0 0 0 88 60 27 0 0 0;
      65 0 0 0 0 37 0 22 0 0 0 33 0 0 0;
      43 32 0 0 0 0 22 0 0 0 0 0 0 19 0 47;
      0 33 0 0 0 0 0 0 0 0 0 0 0 0 32;
      0 0 0 21 35 0 0 0 0 0 0 0 0 0 0;
      0 0 0 0 37 88 0 0 0 0 74 0 0 0 0;
      0 0 0 0 0 60 0 0 0 0 74 0 0 0 0;
      0 0 0 0 0 27 33 0 0 0 0 0 0 0 0;
      0 0 0 0 0 0 19 0 0 0 0 0 0 35 36;
      0 0 0 0 0 0 0 0 0 0 0 0 35 0 19;
      0 0 0 0 0 0 0 47 32 0 0 0 0 36 19 0];
```

```
[d P] = dijkstra (G,12,8)
```

The result is

d = 119

P = 8 7 6 12

That is, the results indicate that a shortest path from Monywa to Sagaing is (Monywa, Chaung-U, Myinmu, Sagaing) and a shortest distance is 119km.

VI. CONCLUSION

There are several government and private organisations in a town whose cars must operate one or more times a day between two designated town places. The organisations can considerably save their costs, time and other resources by using the shortest paths and can also enhance the organizations' productivity and effectiveness. In addition, some graph theory applications are helpful in discrete mathematics, computer science, and other applications.

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Table II. List Representation Of Partial Road-network Of Figure

Vertex	adjacent vertices	are length	adjacent vertex	are length	adjacent vertex	are length	adjacent vertex	are length	adjacent vertex	are length	adjacent vertex	are length	adjacent vertex	are length	adjacent vertex
1	7	51	2	70	3	84	4	60	5	46	6	65	7	43	8
2	3	51	1	38	3	33	9								
3	3	70	1	38	2	14	4								
4	4	84	1	14	3	37	5	21	10						
5	4	60	1	37	4	35	10	37	11						
6	5	46	1	37	7	88	11	60	12	27	13				
7	4	65	1	37	6	22	8	33	13						
8	5	43	1	32	2	22	7	19	14	47	16				
9	2	33	2	32	16										
10	2	21	4	35	5										
11	3	37	5	88	6	74	12								
12	2	60	6	74	11										
13	2	27	6	33	7										
14	3	19	8	35	15	36	16								
15	2	35	14	19	16										
16	4	47	8	32	9	36	14	19	15						

TABLE II. LIST REPRESENTATION OF PARTIAL ROAD-NETWORK OF FIGURE